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# Electronic structure engineering of tin telluride through co-doping of bismuth and indium for high performance thermoelectrics: a synergistic effect leading to a record high room temperature $ZT$ in tin telluride†

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The ever increasing demand for alternative clean energy sources has led to intense research towards the optimization of thermoelectric performance of known systems. In this work, we engineer the electronic structure of SnTe by co-doping it with Bi and In. The co-doping not only results in the formation of two different resonance states and a reduced valence band offset, as in the case of previously reported co-doped SnTe, but also leads to opening of the band gap, which otherwise was closed in the case of Bi and In doped SnTe configurations, leading to suppression of bipolar diffusion. The synergistic action of all these effects leads to an increased Seebeck co-efficient throughout the temperature range and a  $ZT_{\max}$  of  $\sim 1.32$  at 840 K. This strategy of co-doping two different resonant dopants resulted in a record high room temperature  $ZT$  of  $\sim 0.25$  at 300 K for SnTe based materials. This work suggests that appropriate combination of dopants to engineer the electronic structure of a material can lead to unpredictable results.

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## 1. Introduction

Thermoelectric (TE) materials with the potential to convert waste heat into electricity have made a name in clean energy sources.<sup>1–3</sup> Metal chalcogenides, particularly lead-free SnTe, have been recently sought after for resolving the world-wide energy crisis due to their tunable TE properties.<sup>1,2,4</sup> The dimensionless figure of merit,  $ZT$ , which is given by  $ZT = \sigma S^2 T / \kappa$ , where  $\sigma$  is electrical conductivity,  $S$  is the Seebeck co-efficient and  $\kappa$  is total thermal conductivity, governs the TE efficiency of a material. The conflicting nature of the terms involved makes optimization of  $ZT$  a tricky problem. Hence, there is an urgent need to develop strategies to either come up with new materials with intriguing properties or improve the properties of the existing TE materials.<sup>5–7</sup>

Although SnTe on its own has a very small value for  $ZT$ , various strategies have been implemented in the past to

improve its efficiency for application as a TE material.<sup>1</sup> Doping and co-doping of various elements for carrier concentration optimization, electronic structure engineering and nanostructuring have been implemented to improve the power factor as well as to decrease the total thermal conductivity of the material.<sup>2</sup> Co-doping of SnTe with Ag–In, Ca–In, Cd–In, Hg–In, Mg–In, and Mn–In has been particularly useful as it is able to simultaneously introduce a resonance level as well as decrease the energy difference between valence sub-bands, which synergistically leads to an enlarged  $ZT$  of about  $\sim 1.65$  at 840 K in the case of Ca–In co-doped SnTe, which is by far the maximum value in the case of SnTe based materials.<sup>8–14</sup> Although in the above mentioned cases doping of M (M = Ag, Ca, Cd, Hg, Mg, and Mn) individually in SnTe enlarges the band gap, co-doping of M and In generally decreases or completely closes the band gap. However, it may be noted here that the effect of co-doping two resonant dopants has not been reported.

Bi doping in SnTe is known to modulate the carrier concentration of SnTe and enhance the  $S$  values while In is known to introduce a resonance level and thereby improve the  $S$  values.<sup>15,16</sup> Herein, we study co-doping of Bi and In in SnTe and its effect on the TE properties both theoretically and experimentally. The effect of co-doping Bi–In in SnTe on the electronic structure was studied using first principles density functional theory (DFT) simulations. Bi–In co-doped SnTe was prepared through sealed tube melting reactions keeping the ratio of Bi to In as 2 : 1 (see the ESI† for details on methods).

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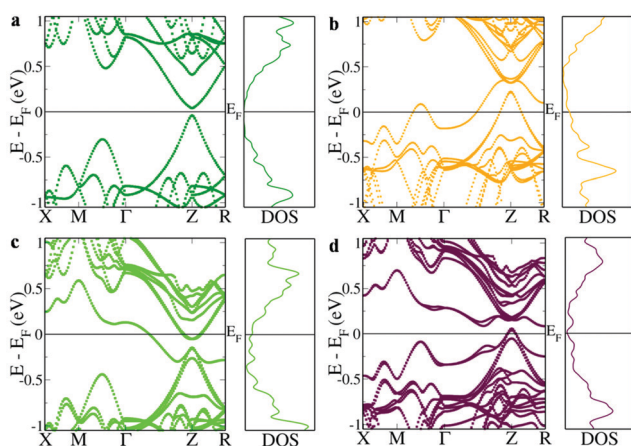
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† Electronic supplementary information (ESI) available: Methods, partial density of states showing contributions of various orbitals, TEM images, elemental composition from EDS results, the Pisarenko plot, variation of theoretically calculated Seebeck coefficient with chemical potential, and variation of power factor, lattice thermal conductivity and  $ZT$  with temperature. See DOI: 10.1039/c9tc01184f

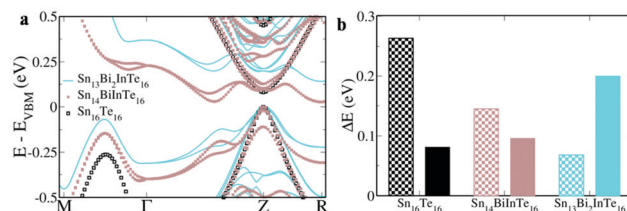
## 2. Results and discussion

The first principles DFT calculations of the electronic structure of a  $2 \times 2 \times 1$  supercell of SnTe revealed a direct band gap of 0.081 eV with conduction and valence band edges symmetric through the gap at the Z point and an energy difference of 0.263 eV between the light hole (at the Z point) and the heavy hole (at the  $M + \delta$  point along the  $M \rightarrow \Gamma$  direction) valence sub-bands (Fig. 1a). The valence band is primarily constituted by Te 'p' orbitals while the conduction bands have a predominant Sn 'p' character (Fig. S1, ESI<sup>†</sup>). Fig. 1b shows the electronic structure of  $\text{Sn}_{15}\text{InTe}_{16}$  wherein the valence band maximum (VBM) splits off as resonance levels and shuts down the band gap, as well documented in the previous literature.<sup>8,9</sup> The appearance of a hump within the valence band in the density of state (DOS) plot due to the In 's' orbital confirms the presence of the resonance level (Fig. S2, ESI<sup>†</sup>).<sup>10</sup> The hybridization between the In 's' orbital and Te 'p' orbitals in the 'deep defect states' appearing at the Fermi level around  $\sim 0$  eV and 'hyperdeep defect states' appearing around  $\sim -5.5$  eV can be clearly seen in Fig. S1 and S2 (ESI<sup>†</sup>) showing the dramatic change in the appearance of the Te 'p' orbitals in the presence of In. The electronic structure of  $\text{Sn}_{15}\text{BiTe}_{16}$  reveals that doping of Bi in SnTe disturbs the degeneracy of the conduction band minimum (CBM) and the impurity induced band appears as resonance states and closes the band gap at the Z point (Fig. 1c). This observation of shutting down the band gap agrees very well with the previously reported Bi doped SnTe.<sup>17</sup> The impurity induced band appears as a hump below the CBM in the DOS plot due to the contribution from the Bi 'p' orbitals (Fig. S2, ESI<sup>†</sup>). We see that the Fermi level lies in the conduction band, making it an n-type material.<sup>17</sup> This nature of Bi impurity induced resonance states is seen in the case of PbTe also.<sup>18</sup> We see that in SnTe, the resonance states introduced by 'p' valence electron impurities

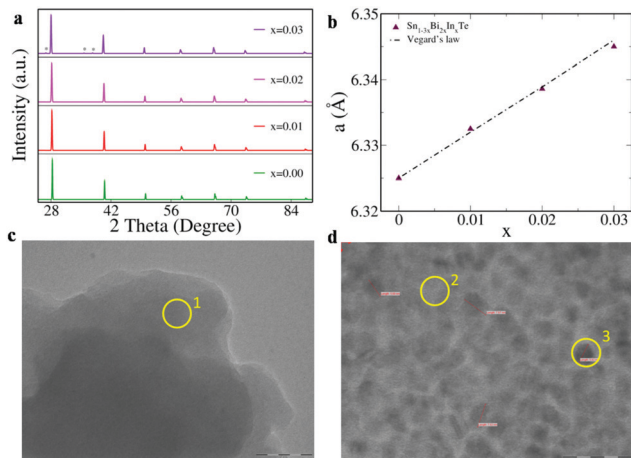
are rather broader than that of the 's' valence electron impurities, as in the case of PbTe.<sup>18</sup> When Bi and In are simultaneously co-doped in SnTe, we see an unexpected change in the electronic structure. The electronic structure of  $\text{Sn}_{14}\text{BiInTe}_{16}$  shows the presence of resonance levels due to both Bi and In (Fig. 1d). It also reveals that the initially eight fold degenerate band (due to spin orbit coupling) of SnTe splits into four two-fold degenerate bands due to the co-doping of In and Bi. Prominent humps are seen in the DOS plot, which could be matched with the contribution from the In 's' orbital for the resonance states closer to the VBM and that from the Bi 'p' states for the resonance level near the CBM (Fig. S3, ESI<sup>†</sup>). Here also we see contributions from the Te 'p' orbitals to the localized bands due to the hybridization as in the individual doping cases (Fig. S1, ESI<sup>†</sup>). The interesting feature to be noted here is that although both Bi and In when individually doped close the band gap of SnTe, when co-doped, the principal band gap at the Z point increases to 0.096 eV. In previously reported Ag–In and Ca–In co-doped SnTe, the principal band gap, which is enlarged due to Ag/Ca doping, shuts down when co-doped with In.<sup>8,9</sup> Although there is a large increase in the band gap due to doping of Cd/Mn in SnTe, co-doping it along with In resulted in the decrease of the band gap.<sup>10,14</sup> Previously, when Ag was co-doped along with Bi in SnTe, there also we saw that the impurity induced band due to Bi got pulled down so much lower that it resulted in a larger overlap with the valence band despite Ag having the ability to increase the band gap.<sup>17</sup> To the best of our knowledge, this is the first case where we see that co-doping of Bi and In enlarges the band gap in the co-doped configuration. When co-doping of Bi and In is done in a 2 : 1 ratio, *viz.*  $\text{Sn}_{13}\text{Bi}_2\text{InTe}_{16}$ , we see that the band gap further enlarges to 0.2 eV (Fig. 2). This shows that the right combination of co-dopants is essential in order to enlarge the band gap since a larger band gap is very much essential to counteract the detrimental effect of bipolar diffusion on the Seebeck as well as thermal conductivity values. When the ratio of Bi and In is changed from 1 : 1 to 2 : 1, we see that the edges of light and heavy hole valence sub-bands approach each other further with the energy difference decreasing to 0.068 eV for the 2 : 1 configuration from the calculated value of 0.145 eV for the 1 : 1 configuration. Due to the above said facts, the 2 : 1 ratio for co-doping was maintained during the synthesis of samples.



**Fig. 1** Electronic structure and DOS of (a)  $\text{Sn}_{16}\text{Te}_{16}$ , (b)  $\text{Sn}_{15}\text{InTe}_{16}$ , (c)  $\text{Sn}_{15}\text{BiTe}_{16}$ , and (d)  $\text{Sn}_{14}\text{BiInTe}_{16}$ . The principal band gap occurring at the L point folds onto the Z point and the heavy hole valence band occurring at the  $\Sigma$  point folds on the  $M + \delta$  point along the  $M \rightarrow \Gamma$  direction due to the dimensions of the supercell ( $2 \times 2 \times 1$ ) used. The resonant states can clearly be identified in the form of humps in the respective DOS for the doped and co-doped configurations.



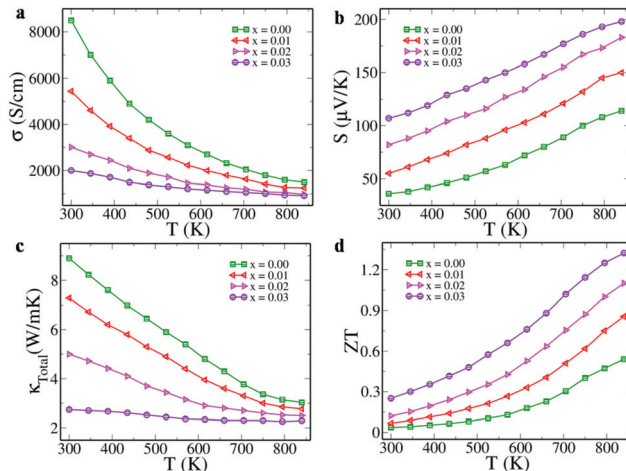
**Fig. 2** Comparison of (a) electronic structures and (b) band gaps (solid bars) and energy differences between light and heavy hole valence subbands (checked bars) of  $\text{Sn}_{16}\text{Te}_{16}$ ,  $\text{Sn}_{14}\text{BiInTe}_{16}$  and  $\text{Sn}_{13}\text{Bi}_2\text{InTe}_{16}$ . The increase in the band gap and the decrease in the energy offset of valence subbands are clearly seen in the electronic structure as the Bi–In ratio changes from 1 : 1 to 2 : 1. In the electronic structure, the energies are shifted with respect to the energy of the valence band maximum (VBM), which is set at zero.



**Fig. 3** (a) Powder XRD pattern; \* in the uppermost panel indicates peaks due to Bi precipitates. (b) Variation of lattice parameter 'a' of  $\text{Sn}_{1-3x}\text{Bi}_{2x}\text{In}_x\text{Te}$  versus dopant concentration 'x'. TEM images of (c)  $\text{Sn}_{0.94}\text{Bi}_{0.04}\text{In}_{0.02}\text{Te}$  and (d)  $\text{Sn}_{0.91}\text{Bi}_{0.06}\text{In}_{0.03}\text{Te}$  showing nanoparticle formation when  $x = 0.03$ . The scale in 'c' measures 50 nm and in 'd' measures 20 nm. The percentage elemental composition of the area marked in the yellow circle is given in Table S1 (ESI†).

Fig. 3a reveals the powder X-ray diffraction pattern of  $\text{Sn}_{1-3x}\text{Bi}_{2x}\text{In}_x\text{Te}$  ( $x = 0.00$  to  $0.03$ ), which could be indexed to the face centered cubic structure of sodium chloride (space group  $Fm\bar{3}m$ ). For the  $x = 0.03$  composition, deviation from a single phase is observed as we see extra peaks appearing that could be indexed to a Bi precipitate. Since the ionic radius of  $\text{Bi}^{3+}$  is higher than  $\text{Sn}^{2+}$  by  $0.03 \text{ \AA}$  and that of In is comparable to Sn, we see a linear increase in the lattice parameter for the co-doped compositions (Fig. 3b).<sup>9</sup> The TEM images reveal that for the  $x = 0.03$  composition, Bi precipitates (around 2–10 nm in size) start appearing that are absent at lower concentrations of doping (Fig. 3c, d and Fig. S4, ESI†). The elemental composition for various spots encircled in the TEM image, obtained *via* energy dispersive spectrometry (EDS), is given in Table S1 (ESI†).

Electrical conductivity values of  $\text{Sn}_{1-3x}\text{Bi}_{2x}\text{In}_x\text{Te}$  as a function of temperature and doping concentration were observed to decrease (Fig. 4a). The decrease with respect to the increase in the temperature is due to the degenerate semiconducting nature while the decrease in value with an increase in the dopant concentration is due to the decrease in the carrier concentration from  $4.1 \times 10^{20} \text{ cm}^{-3}$  ( $x = 0.00$ ) to  $2.9 \times 10^{20} \text{ cm}^{-3}$  ( $x = 0.03$ ). The formation of resonance states by both Bi and In, opening of the band gap and approaching of the valence sub-band edges towards each other as revealed by the DFT calculations have a profound impact on the Seebeck co-efficient values (Fig. 4b). The room temperature values of  $S$  increase from  $36 \mu\text{V K}^{-1}$  ( $x = 0.00$ ) to  $107 \mu\text{V K}^{-1}$  ( $x = 0.03$ ) and a maximum of  $198 \mu\text{V K}^{-1}$  at 840 K is reached for  $x = 0.03$ . Comparison of the room temperature values of  $S$  with the Pisarenko plot reported by Zhang *et al.* (Fig. S5, ESI†) reveals that the  $S$  value for pristine SnTe falls exactly on top of the line while those of the co-doped samples are much higher than the predicted values.<sup>16</sup> This is attributed to the increase in band effective mass due to the



**Fig. 4** Variation of (a) electrical conductivity, (b) Seebeck coefficient, (c) thermal conductivity, and (d)  $ZT$  with temperature in  $\text{Sn}_{1-3x}\text{Bi}_{2x}\text{In}_x\text{Te}$ . The positive value of the Seebeck coefficient reveals that holes are the majority carriers leading to p-type conduction in the material.

resonant states introduced by both Bi and In. Also, the decrease in the separation of light and heavy hole valence bands as determined by the DFT study increases the valley degeneracy from 4 to 16 (4 from light and 12 from heavy hole bands) and hence increases the Seebeck values.<sup>12</sup> The effect of dopants on the Seebeck values was also determined theoretically using the Boltztrap code.<sup>19</sup> The variation of calculated Seebeck coefficient as a function of chemical potential ( $\mu$ ) in the temperature range of 300–800 K is shown in Fig. S6 (ESI†). The negative and positive chemical potentials indicate the hole and electron doping corresponding to p and n-type doping, respectively. At a particular value of  $\mu$ , the value of  $S$  increases with an increase in temperature. The positive Seebeck peak is found in the negative chemical potential region in Bi doped SnTe due to the Fermi level lying almost at the tip of the conduction band with a resonant peak lying below the Fermi level (Fig. S6a, ESI†). In the case of In doped SnTe, the positive Seebeck peak lies in the positive chemical potential region because of the presence of the Fermi level in the valence band and the resonance level appearing above the Fermi level (Fig. S6b, ESI†). This indicates that the resonance states are responsible for the increase in the  $S$  values in both cases. The Seebeck peak lies in the positive potential range closer to the Fermi level due to the Fermi level residing at the top of the valence band, as revealed in the electronic structure (Fig. S6c, ESI†). The features of both singly doped configurations are present in the co-doped configuration. The co-doped SnTe configuration exhibits a higher Seebeck coefficient at larger potential windows at higher temperatures. These results suggest that  $ZT$  can be improved for a wide range of carrier concentrations at higher temperatures. Further, this observation also indirectly supports the fact that bipolar diffusion is prevented due to the larger band gap of the co-doped sample.

A maximum power factor (given by  $\sigma S^2$ ) of  $\sim 36 \mu\text{W cm}^{-1} \text{ K}^{-2}$  was observed when  $x = 0.03$  at 840 K (Fig. S7, ESI†), which is appreciably higher than the optimized compositions of Bi doped

SnTe ( $\sim 20 \mu\text{W cm}^{-1} \text{K}^{-2}$ ) and In doped SnTe ( $\sim 21 \mu\text{W cm}^{-1} \text{K}^{-2}$ ) reported previously.<sup>15,16</sup> Although the electrical conductivity decreases with increasing temperature, the large increase in  $S$  value makes the power factor increase as a function of temperature and dopant fraction. The total thermal conductivity of the samples decreases as a function of temperature and dopant concentration (Fig. 4c). The lattice thermal conductivity was obtained by subtracting the electronic thermal conductivity from the total thermal conductivity. The lattice thermal conductivity shows a decreasing trend with increasing temperature and dopant concentration (Fig. S8, ESI†). This indicates that the dopants effectively scatter the heat carrying phonons due to mass contrast. Moreover, the formed Bi nanoprecipitates in the  $\text{Sn}_{1-3x}\text{Bi}_{2x}\text{In}_x\text{Te}$  ( $x = 0.03$ ) sample further scatter the additional phonons causing the decrease in the thermal conductivity values.<sup>5</sup> Also, the increase in the band gap of the material, as revealed by DFT studies, prevents the bipolar thermal transport from further decreasing the total thermal conductivity.

We see that the  $ZT$  value increases both as a function of temperature and dopant concentration (Fig. 4d). We report here a record high room temperature  $ZT$  of  $\sim 0.25$  at 300 K, higher than the previously reported record high value of  $\sim 0.2$  for Ca doped SnTe.<sup>20</sup> The result of all these thermal transport properties is the  $ZT_{\text{max}}$  value of  $\sim 1.32$  attained at 840 K for  $x = 0.03$  and  $ZT_{\text{avg}}$  of  $\sim 0.73$ , considering 300 and 840 K as cold and hot ends, respectively. These values are comparable to the  $ZT_{\text{max}}$  value of  $\sim 1.4$  at 923 K and  $ZT_{\text{avg}}$  of  $\sim 0.78$  between 300 and 900 K reported for Cd–In co-doped SnTe. Our reported  $ZT_{\text{max}}$  is also comparable to the value of  $\sim 1.4$  (at 773 K) recently reported for In–I co-doped PbTe. Notably, our material has the advantage of being free from toxic Cd and Pb and is hence more environmentally benign.<sup>10,21</sup> The reported  $ZT_{\text{max}}$  value is higher than the previously reported values for SnTe singly doped with In ( $\sim 1.1$  at 873 K) and Bi ( $\sim 1.1$  at 873 K), and co-doped with Ag–In ( $\sim 1$  at 856 K), Cd–In ( $\sim 1.1$  at 850 K), Hg–In ( $\sim 0.9$  at 850 K), and Mn–In ( $\sim 1.03$  at 923 K), and  $\text{Sn}_{1-x}\text{Pb}_x\text{Te}$  ( $x = 0.3$ ) co-doped with Mg–In ( $\sim 1$  at 710 K).<sup>8,11,13–16,22</sup> The  $ZT$  values of the Bi–In co-doped SnTe are found to be much higher than the Bi/In singly doped SnTe, as revealed in Fig. S9 (ESI†), indicating the synergistic effect of the dopants. Although the reported value of  $ZT_{\text{max}}$  in the present work is lower than the one reported for Ca–In co-doped SnTe ( $\sim 1.65$  at 840 K), which by far holds the record in SnTe based materials, the  $ZT_{\text{avg}}$  value reported here is  $\sim 0.95$ , much higher than  $\sim 0.87$  reported for Ca–In co-doped SnTe for the same temperature range of 500–840 K, indicating its higher potential for thermoelectric application, as the efficiency of a TE device depends more on  $ZT_{\text{avg}}$  than  $ZT_{\text{max}}$ .<sup>9</sup>

### 3. Conclusions

In this work, we engineer the electronic structure of SnTe by co-doping it with Bi and In using first principles DFT simulations and experiments. For the first time, we report that Bi introduces resonance states in SnTe. We see that the co-doping of two

different resonant dopants not only results in edges of valence sub-bands approaching one another but also leads to opening of the band gap, which otherwise was closed in the case of the doped Bi and In configurations. This leads to an increased Seebeck co-efficient throughout the temperature range and reduced thermal conductivity at elevated temperatures due to the suppression of the bipolar diffusion and the formation of nanoprecipitates at  $x = 0.03$  in  $\text{Sn}_{1-3x}\text{Bi}_{2x}\text{In}_x\text{Te}$ . The synergistic action of all these effects makes the material achieve a record high room temperature  $ZT$  of  $\sim 0.25$  at 300 K for SnTe based materials and a maximum  $ZT$  of  $\sim 1.32$  at 840 K, making it a promising thermoelectric material. This strategy of co-doping n-type and p-type resonant dopants to increase the band gap of SnTe and to introduce deep defect states to improve  $ZT$  throughout the temperature range can potentially be used for other materials as well.

### Conflicts of interest

There are no conflicts of interest to declare.

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### References

- 1 S. Li, X. Li, Z. Ren and Q. Zhang, Recent progress towards high performance of tin chalcogenide thermoelectric materials, *J. Mater. Chem. A*, 2018, **6**, 2432–2448.
- 2 R. Moshwan, L. Yang, J. Zou and Z. G. Chen, Eco-friendly SnTe thermoelectric materials: progress and future challenges, *Adv. Funct. Mater.*, 2017, **27**, 1703278.
- 3 Y. Liu, W. Wang, J. Yang and S. Li, Recent advances of layered thermoelectric materials, *Adv. Sustainable Syst.*, 2018, **2**, 1800046.
- 4 P. Ren, Y. Liu, J. He, T. Lv, J. Gao and G. Xu, Recent advances in inorganic material thermoelectrics, *Inorg. Chem. Front.*, 2018, **5**, 2380–2398.
- 5 X. Zhou, Y. Yan, X. Lu, H. Zhu, X. Han, G. Chen and Z. Ren, Routes for high-performance thermoelectric materials, *Mater. Today*, 2018, **21**, 974–988.
- 6 S. U. Shenoy and D. K. Bhat, Enhanced bulk thermoelectric performance of  $\text{Pb}_{0.6}\text{Sn}_{0.4}\text{Te}$ : effect of magnesium doping, *J. Phys. Chem. C*, 2017, **121**, 20696–20703.
- 7 A. Banik, U. S. Shenoy, S. Anand, U. V. Waghmare and K. Biswas, Mg Alloying in SnTe Facilitates Valence Band Convergence and Optimizes Thermoelectric Properties, *Chem. Mater.*, 2015, **27**, 581–587.
- 8 A. Banik, U. S. Shenoy, S. Saha, U. V. Waghmare and K. Biswas, High Power Factor and Enhanced Thermoelectric Performance of  $\text{SnTe-AgInTe}_2$ : Synergistic Effect of Resonance



- Level and Valence Band Convergence, *J. Am. Chem. Soc.*, 2016, **138**, 13068–13075.
- 9 D. K. Bhat and S. U. Shenoy, Enhanced thermoelectric performance of bulk tin telluride: synergistic effect of calcium and indium co-doping, *Mater. Today Phys.*, 2018, **4**, 12–18.
- 10 G. Tan, F. Shi, S. Hao, H. Chi, L. D. Zhao, C. Uher, C. Wolverton, V. P. Dravid and M. G. Kanatzidis, Codoping in SnTe: Enhancement of Thermoelectric Performance through Synergy of Resonance Levels and Band Convergence, *J. Am. Chem. Soc.*, 2015, **137**, 5100–5112.
- 11 X. Tan, X. Tan, G. Liu, J. Xu, H. Shao, H. Hu, M. Jin, H. Jiang and J. Jiang, Optimizing the thermoelectric performance of In-Cd codoped SnTe by introducing Sn vacancy, *J. Mater. Chem. C*, 2017, **5**, 7504–7509.
- 12 D. K. Bhat and S. U. Shenoy, High thermoelectric performance of co-doped tin telluride due to synergistic effect of magnesium and indium, *J. Phys. Chem. C*, 2017, **121**, 7123–7130.
- 13 X. Tan, G. Liu, J. Xu, X. Tan, H. Shao, H. Hu, H. Jiang, Y. Lu and J. Jiang, Thermoelectric properties of In-Hg co-doping in SnTe: energy band engineering, *J. Materiomics*, 2018, **4**, 62–67.
- 14 H. Wang, J. Hwang, C. Zhang, T. Wang, W. Su, H. Kim, J. Kim, J. Zhai, X. Wang, H. Park, W. Kim and C. Wang, Enhancement of the thermoelectric performances of bulk SnTe alloys via the synergistic effect of band structure modification and chemical bond softening, *J. Mater. Chem. A*, 2017, **5**, 14165–14173.
- 15 Z. Zhou, J. Yang, Q. Jiang, Y. Luo, D. Zhang, Y. Ren, X. He and J. Xin, Multiple effects of Bi doping in enhancing the thermoelectric properties of SnTe, *J. Mater. Chem. A*, 2016, **4**, 13171–13175.
- 16 Q. Zhang, B. Liao, Y. Lan, K. Lucas, W. Liu, K. Esfarjani, C. Opeil, D. Broido, G. Chen and Z. Ren, High Thermoelectric Performance by Resonant Dopant Indium in Nanostructured SnTe, *Proc. Natl. Acad. Sci. U. S. A.*, 2013, **110**, 13261–13266.
- 17 K. Hoang, S. D. Mahanti and M. G. Kanatzidis, Impurity clustering and impurity-induced bands in PbTe-, SnTe- and GeTe-based bulk thermoelectrics, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2010, **81**, 115106.
- 18 S. Ahmad, S. D. Mahanti, K. Hoang and M. G. Kanatzidis, Ab initio studies of the electronic structure of defects in PbTe, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2006, **74**, 155205.
- 19 G. K. H. Madsen and D. J. Singh, BoltzTrap. A code for calculating band structure dependent quantities, *Comput. Phys. Commun.*, 2006, **175**, 67–71.
- 20 R. A. R. A. Orabi, N. A. Mecholsky, J. Hwang, W. Kim, J. S. Rhyee, D. Wee and M. Fornari, Band Degeneracy, Low Thermal Conductivity, and High Thermoelectric Figure of Merit in SnTe-CaTe Alloys, *Chem. Mater.*, 2016, **28**, 376–384.
- 21 Q. Zhang, Q. Song, X. Wang, J. Sun, Q. Zhu, K. Dahal, X. Lin, F. Cao, J. Zhou, S. Chen, G. Chen, J. Mao and Z. Ren, Deep defect level engineering: a strategy of optimizing the carrier concentration for high thermoelectric performance, *Energy Environ. Sci.*, 2018, **11**, 933–940.
- 22 S. Roychowdhury, U. S. Shenoy, U. V. Waghmare and K. Biswas, An enhanced seebeck coefficient and high thermoelectric performance in p-type In and Mg co-doped  $\text{Sn}_{1-x}\text{Pb}_x\text{Te}$  via the co-adjutant effect of the resonance level and heavy hole valence band, *J. Mater. Chem. C*, 2017, **5**, 5737–5748.